

## 1 ER Diagrams

We want to store sports teams and their players in our database. Draw an ER diagram corresponding to data given below:

- Every Team in our database will have a unique team\_name and a stadium where they play their games.
- Each Coach has a name.
- Each Player will have a player\_id, name and their average score.
- Our database will contain who Plays\_For which team and also the “position” that the player plays in. We also need to store who Captains a team, and who Coaches a team.
- Every Team needs players, and needs exactly one captain.
- Each Player can be on at most one team, but may currently be a free agent and not on any team.
- Each team needs coaches and may have many.
- A Coach is uniquely identified by which team they coach.

## 2 Functional Dependencies

- When there's a lot of symbols floating around, it's best to keep track of the "type" of the various symbols and expressions. Consider a set of functional dependencies  $F = \{X \rightarrow Y, Y \rightarrow Z\}$ . For each of the following symbols or expressions, indicate whether it is (a) an attribute, (b) a set of attributes, (c), a set of sets of attributes, (d) a functional dependency, (e) a set of functional dependencies, or (f) none of the above.

- X
- XY
- $X \rightarrow Y$
- F
- $F^+$
- $X^+$
- Armstrong's reflexivity axiom

- Consider a relation  $R(x, y, z)$  and the list of functional dependencies  $X \rightarrow Y$ ,  $XY \rightarrow YZ$ , and  $Y \rightarrow X$  where  $X = \{x\}$ ,  $Y = \{y\}$ , and  $Z = \{z\}$ . For each of the following relations, indicate which functional dependencies it might satisfy.

x	y	z
1	2	0
1	2	1
1	3	0
2	3	0

x	y	z
1	2	1
1	3	1
2	3	0

x	y	z
1	3	1
2	3	0

x	y	z
1	3	1

- Consider the set  $F = \{A \rightarrow B, AB \rightarrow AC, BC \rightarrow BD, DA \rightarrow C\}$  of functional dependencies. Compute the following attribute closures.

- $A^+$
- $B^+, C^+, D^+$
- $AB^+, AC^+, AD^+$
- $BC^+$
- $BD^+$
- $CD^+$
- $BCD^+$

4. Consider again the set  $F$  of functional dependencies from Question 3. Indicate whether the following sets of attributes are candidate keys, superkeys (but not candidate keys), or neither.
- (a)  $A$
  - (b)  $B, C, D$
  - (c)  $AB, AC, AD$
  - (d)  $BC$
  - (e)  $BD$
  - (f)  $CD$
  - (g)  $BCD$

### 3 Normal Forms

1. Decompose  $R = ABCDEFG$  into BCNF, given the functional dependency set:  $F = AB \rightarrow CD, C \rightarrow EF, G \rightarrow A, G \rightarrow F, CE \rightarrow F$ .
  
2. Does the above decomposition preserve dependencies? Why/why not?