

1 Assorted Joins

- Companies: (company_id, industry, ipo_date)
- NYSE: (company_id, date, trade, quantity)

We have 20 pages of memory, and we want to join two tables Companies and NYSE on $C.\text{company_id} = N.\text{company_id}$. Attribute `company_id` is the primary key for Companies. For every tuple in Companies, assume there are 4 matching tuples in NYSE.

NYSE contains $[N] = 100$ pages, NYSE holds $pN = 100$ tuples per page.

Companies contains $[C] = 50$ pages, C holds $pC = 50$ tuples per page.

There are unclustered B+ indexes on $C.\text{company_id}$ and $N.\text{company_id}$ – for both indexes, assume it takes 2 I/Os to access a leaf.

(a) How many disk I/Os are needed to perform a simple nested loops join?

$$[C] + pC * [C] * [N] = 50 + 50 * 50 * 100 = 250050$$

(b) How many disk I/Os are needed to perform an index nested loops join?

$$[C] + [C] * pC * (\text{cost to find matching NYSE tuples}) = 50 + 50 * 50 * (2 + 4) = 15,050$$

(c) How many disk I/Os are needed to perform a block nested loops join?

$$\begin{aligned} & (\# \text{ pages in smaller relation}) + \text{ceil}[(\# \text{ pages in smaller relation}) / (\# \text{ pages in memory} - 2)] * \\ & (\# \text{ pages in larger relation}) = 50 + \text{ceil}(50/18) * 100 = 350 \text{ I/Os} \end{aligned}$$

(d) How many disk I/Os are needed to perform a sort merge join? This is ordinary sort-merge, not optimized sort-merge.

$$\begin{aligned} \text{Sorting C: } & 4 * (50 \text{ pages}) = 200 \text{ I/Os} \\ \text{Sorting N: } & 4 * (100 \text{ pages}) = 400 \text{ I/Os} \\ \text{Joining: } & [C] + [N] = 150 \text{ I/Os} \\ \text{Total: } & 200 + 400 + 150 = 750 \text{ I/Os} \end{aligned}$$

(e) How many disk I/Os are needed to perform a hash join?

No recursive partitioning required.
Partitioning phase:
 $\text{ceil}([N]/(B - 1)) = 6$ pages per partition for N
 $\text{ceil}([C]/(B - 1)) = 3$ pages per partition for C

$$([N] + [C]) + ((B - 1) * (6 + 3)) = 321 \text{ I/Os}$$

$$\text{Probing phase: } (B - 1) * (6 + 3) = 171 \text{ I/Os}$$

$$\text{Total: } 321 + 171 = 492 \text{ I/Os}$$

- (f) Now assume the index on NYSE.company_id is clustered. What is the cost of an index nested loops join using companies as the outer relation?

$$[C] + [C]*pC * (\text{cost to find matching NYSE tuples}) = 50 + 50 * 50 * (2 + \text{ceil}(4/100)) \\ = 7,550 \text{ I/Os}$$

2 Grace Hash Join

We have 2 tables – Catalog and Transactions.

Catalog has a total of 100 pages and 20 tuples per page. Transactions has a total of 50 pages and 50 tuples per page. Assume that the distribution among the key that we are joining on is uniform for the two tables.

- (a) If we had 10 buffer pages, how many partitioning phases would we require for grace hash join? Consider which table we should build the hash table in the probing phase on.

T is smaller, need partitions of T to be at most $B - 2 = 8$ pages.

After 1 partitioning pass, we have partitions of size 6, which is small enough.

- (b) What is the I/O cost for the grace hash join then? Assume uniform partitioning.

We need 1 partitioning pass.

Partitioning phase:

$$\text{ceil}([C]/(B - 1)) = 12 \text{ pages per partition for C}$$

$$\text{ceil}([T]/(B - 1)) = 6 \text{ pages per partition for T}$$

$$([C] + [T]) + ((B - 1) * (12 + 6)) = 312 \text{ I/Os}$$

$$\text{Probing phase: } (B - 1) * (12 + 6) = 162 \text{ I/Os}$$

$$\text{Total: } 312 + 162 = 474 \text{ I/Os}$$

- (c) For the above question, if we only had 8 buffer pages, how many number of partition phases would there be?

T is smaller, need partitions of T to be at most $B - 2 = 6$ pages.

After 1 partitioning pass, we have partitions of size 8, which is too big. We need a second partitioning pass.

- (d) What will be the I/O cost? Assume uniform partitioning.

We need 2 partitioning passes.

Partitioning phase:

$$\text{ceil}([C]/(B - 1)) = 15 \text{ pages per partition for C}$$

$$\text{ceil}([T]/(B - 1)) = 8 \text{ pages per partition for T}$$

$$\text{ceil}([C]/(B - 1)) = 3 \text{ pages per partition for second pass for C}$$

$$\text{ceil}([T]/(B - 1)) = 2 \text{ pages per partition for second pass for T}$$

$$([C] + [T]) + 2 * ((B - 1) * (15 + 8)) + ((B - 1) * (B - 1) * (3 + 2)) = 150 + 2 * 161 + 245 \\ = 717 \text{ I/Os}$$

$$\text{Probing phase: } ((B - 1) * (B - 1) * (3 + 2)) = 245 \text{ I/Os}$$

$$\text{Total: } 717 + 245 = 962 \text{ I/Os}$$