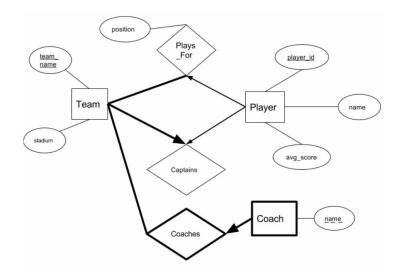
## 1 ER Diagrams

We want to store sports teams and their players in our database. Draw an ER diagram corresponding to data given below:

- Every Team in our database will have a unique team\_name and a stadium where they play their games.
- Each Coach has a name.
- Each Player will have a player\_id, name and their average score.
- Our database will contain who Plays\_For which team and also the "position" that the player plays in. We also need to store who Captains a team, and who Coaches a team.
- Every Team needs players, and needs exactly one captain.
- Each Player can be on at most one team, but may currently be a free agent and not on any team.
- Each team needs coaches and may have many.
- A Coach is uniquely identified by which team they coach.



## 2 Functional Dependencies

- 1. When there's a lot of symbols floating around, it's best to keep track of the "type" of the various symbols and expressions. Consider a set of functional dependencies F = {X -> Y, Y -> Z}. For each of the following symbols or expressions, indicate whether it is (a) an attribute, (b) a set of attributes, (c), a set of sets of attributes, (d) a functional dependency, (e) a set of functional dependencies, or (f) none of the above.
  - (a) X (b) a set of attributes
  - (b) XY (b) a set of attributes
  - (c) X -> Y (d) a functional dependency
  - (d) F (e) a set of functional dependencies
  - (e) F+ (e) a set of functional dependencies
  - (f) X+ (b) a set of attributes
  - (g) Armstrong's reflexivity axiom (f) an axiom
- 2. Consider a relation R(x, y, z) and the list of functional dependencies  $X \rightarrow Y$ ,  $XY \rightarrow YZ$ , and  $Y \rightarrow X$  where  $X = \{x\}$ ,  $Y = \{y\}$ , and  $Z = \{z\}$ . For each of the following relations, indicate which functional dependencies it might satisfy.

Х	У	Z
<b>X</b>	2 2 3 3	0
1	2	1
1 2	3	0
2	3	0
х	У	z
1 1 2	2 3 3	1 1 0
1	3	1
2	3	0
x	У	z
1 2	<b>y</b> 3	1 0
2	3	0
х	У	z
1	<b>y</b> 3	<b>z</b>

- 1. None
- 2. XY -> YZ
- 3. X -> Y. XY -> YZ
- 4.  $X \rightarrow Y, XY \rightarrow YZ, Y \rightarrow X$
- 3. Consider the set  $F = \{A \rightarrow B, AB \rightarrow AC, BC \rightarrow BD, DA \rightarrow C\}$  of functional dependencies. Compute the following attribute closures.
  - (a) A+ ABCD
  - (b) B+, C+, D+ B, C, D; B, C, and D do not appear alone on the left of any functional dependency, so nothing is in their attribute closures besides themselves.
  - (c) AB+, AC+, AD+ ABCD; A+ = ABCD, so AX = ABCD for any X.

- (d) BC+BCD
- (e) BD+BD
- (f) CD+CD
- (g) BCD+BCD
- 4. Consider again the set F of functional dependencies from Question 3. Indicate whether the following sets of attributes are candidate keys, superkeys (but not candidate keys), or neither.
  - (a) A candidate key
  - (b) B, C, D neither
  - (c) AB, AC, AD superkey
  - (d) BC neither
  - (e) BD neither
  - (f) CD neither
  - (g) BCD neither

## 3 Normal Forms

1. Decompose R = ABCDEFG into BCNF, given the functional dependency set:  $F = AB \rightarrow CD$ ,  $C \rightarrow EF$ ,  $G \rightarrow A$ ,  $G \rightarrow F$ ,  $CE \rightarrow F$ .

AB→CD => decompose ABCDEFG into ABCD, ABEFG

 $G \rightarrow A => decompose ABEFG into AG, BEFG$ 

 $G \rightarrow F => decompose BEFG into FG, BEG$ 

Final relations: ABCD, AG, FG, BEG.

2. Does the above decomposition preserve dependencies? Why/why not?

No,  $C \to EF$  and  $CE \to F$  are not represented in the closure of the union of each subrelation's dependencies.s